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| B.Tech. 5th Semester End-Term Examination |   |   |          |          |           |   |                                      |  |  |
|   |   |   |          |          |           | CS                                      | E.                                   |  |  |
|   |   |   | DE       | SIGN A   | AND AN    | ALYS                                    | SIS OF ALGORITHM                     |  |  |
|   |   |   |          | (New     | Regula    | tion                                    | & New Syllabus)                      |  |  |
| Ful                                       | l Mar   | ks –  | 70       |          |           |   | Time - Three hours                   |  |  |
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|   |   |   | 111      | e ngur   |           |   | gin indicate full marks<br>nestions. |  |  |
|   |   |   |          |          |           |   |                                      |  |  |
|   |   |   | Answ     | er que   | stion No  | . 1 an                                  | d any four from the rest.            |  |  |
| 1.  | Choose the most appropriate choice to answer the following : $(10 \times 1 = 10)$ |   |          |          |           |   |                                      |  |  |
|   | (i) Which of the following is a Divide and Conquer algorithm?                     |   |          |          |           |   |                                      |  |  |
|   |   | (a)   | Buble so | ort      | 14        | (b)                                     | Selection sort                       |  |  |
|   |   | (c)   | Merge s  | ort      |           | (d)                                     | All above                            |  |  |
|   | (ii)  | (ii) What is the worst case time complexity of a quick sort algorithm elements? |          |          |           |   |                                      |  |  |
|   |   | (a)   | O(n)     |          |           | (b)                                     | O(n log n)                           |  |  |
|   |   | (c)   | O(n2)    | -        |           | (d)                                     | O(log n)                             |  |  |
|   | (iii) What is the worst case time complexity of linear search on n elements?      |   |          |          |           |   |                                      |  |  |
|   |   | (a)   | O(nlogn  | )        |           | (b)                                     | O(logn)                              |  |  |
|   |   | (c)   | O(n)     |          |           | (d)                                     | O(1)                                 |  |  |
|   | (iv) Which of the following data structure helps to implement recursion?          |   |          |          |           |   |                                      |  |  |
|   |   | (a)   | Stack    |          |           | (b)                                     | Queue                                |  |  |
|   |   | (c)   | Binary 7 | ree      |           | (d)                                     | None above                           |  |  |
|   |   |   |          |          |           |   | [Turn over                           |  |  |

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| A sorting technique is called stable if  |  |  |  |  |  |  |
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| The concatenation of two lists is to be performed in O(1) time. Which of the ollowing implementations of a list should be used?  |  |  |  |  |  |  |
| Singly linked linear List  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| None of above  |  |  |  |  |  |  |
| Consider following array of elements (89, 19, 50, 17, 12, 15, 2, 5, 7, 11, 6, 9, 100). The minimum number of interchanges needed to convert it into a max binary heap is |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

- (a) For each of the following recurrences, derive an expression for the runtime
   T (n) if the recurrence can be solved with the Master Theorem. Otherwise, indicate why Master Theorem does not apply.
   (5+5=10)
  - (i) T(n)=16T(n/4)+n

(ii)  $T(n)=2T(n/2)+n\log n$ 

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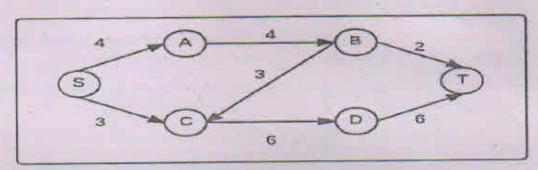
- (b) Analyses the time complexity of Binary Search on a sorted sequence of numbers stored in an array [No need to write algorithm] (5)
- (a) Explain divide and conquer method of Problem solving. Discuss its merits.
  (5)

(b) Consider the following array of numbers (10, 2, 18, 5, 20, 6, 15, 25, 5, 40, 50, 30). Use quick sort to apply divide and conquer method to sort it in ascending order. Analyses the time complexity

- 4. Consider the following array of numbers: (10, 2, 18, 5, 20, 6, 15, 25,5, 40, 50, 30).
  - (a) Construct a max binary heap from this array. (5)
  - (b) Explain how you can implement the max heap as a priority queue on the heap constructed in question 4 (a). Also analyse the time complexity of the insertion and deletion operations on the priority queue. (5+5=10)
- 5. (a) What is the benefit of using Binomial Heap? Construct a binomial heap (min) if the following keys are inserted one after another in the given sequence. 16,9,30,26,8,20,22,5, 12.
  - (b) Analyse the complexities of Breadth First and Depth First search with example. (10)
- 6. (a) Explain with an example how greedy strategies are applied in PRIM's algorithm to find minimum spanning tree. (5)
  - (b) Apply dynamic programming technique to find the optimal parenthesis for the matrix chain multiplication of the following matrix chain: A1 × A2 × A3 × A4, where the dimensions are as follows: (10)

| Matrix | Dimension    |
|--------|--------------|
| A1     | 8 × 4        |
| A2     | 4×2          |
| A3     | $2 \times 6$ |
| A4     | 6×5          |

- (a) What is travelling salesman problem? State a few applications of Travelling salesman problem.
   (5)
  - (b) Following is a flow network, with source S and sink T. The numbers assigned to the edges are the flow capacities of the edges. Apply Ford and Fulkerson algorithm and explain how much "flow" (maximum) can the network process at a time? (No need to write any algorithm). (10)



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